## Ignoring base rates

- People were told that they would be reading descriptions of a group that had 30 engineers and 70 lawyers.
- People had to judge whether each description was of an engineer or a lawyer. They gave a number that reflected their confidence in their judgement.
- They should have factored in the base rate: the overall likelihood that a given case will fall in a given category


## Ignoring base rates (cont.)

- If the description matched people's stereotype of an engineer, they judged that the description was of an engineer
- People's judgments were not influenced by different base rate information (70 engineers and 30 lawyers vs. 70 lawyers and 30 engineers)


## Improving our judgments

- People are more likely to use statistical knowledge when it is triggered by the situation.
- When people had to judge descriptions as belonging to a lawyer vs. engineer, they did better when they drew the descriptions out of a jar -- they made use of base rate information
- Highlighting the role of chance improves judgment.


## When Base Rate Matters

- $85 \%$ of accidents involve green cabs
- $15 \%$ of accidents involve blue cabs
- Witness: Cab was blue.
- Witness: $80 \%$ accurate when ID-ing colors
- What's the probability the cab was blue?
- Survey says: 60\%
- Bayes (still) says: 41\%

Causal scenarios make base rates relevant

## Probabilities vs. Frequencies

The probability of breast cancer is $1 \%$ for a woman at age 40 who participates in routine screening. If a woman has breast cancer, the probability is $80 \%$ that she will get a positive mammography. If a woman does not have breast cancer, the probability is $9.6 \%$ that she will get a positive mammography. A woman in this age group had a positive mammography in a routine screening. What is the probability that she actually has breast cancer?

## Frequency \& Probability Formats for a Bayesian Inference Problem



## The Representativeness Heuristic

- We often judge whether object $X$ belongs to class $Y$ by how representative $X$ is of class Y
- For example, people order the potential occupations by probability and by similarity in exactly the same way
- The problem is that similarity produces multiple biases


## Three Major Heuristics/Biases

(Tversky and Kahneman, 1974)

- Representativeness
- The more object X is similar to class Y , the more likely we think X belongs to Y
- Availability
- The easier it is to consider instances of class Y , the more frequent we think it is
- Anchoring
- Initial estimated values affect the final estimates, even after considerable adjustments


## Representative Bias (1): Insensitivity to Prior Probabilities

- The base rate of outcomes should be a major factor in estimating their frequency
- However, people often ignore it (e.g., there are more farmers than librarians)


## Representative Bias (2): Insensitivity to Sample Size

- The size of a sample withdrawn from a population should greatly affect the likelihood of obtaining certain results in it
- People, however, ignore sample size and only use the superficial similarity measures
- For example, people ignore the fact that larger samples are less likely to deviate from the mean than smaller samples


## Representative Bias (3): Misconceptions of Chance

- Random patterns appear nonrandom \& people may inappropriately attribute a cause for the apparent pattern
- People expect random sequences to be
"representatively random" even locally
- E.g., they consider a coin-toss run of HTHTTH to be more likely than HHHTTT or HHHHTH
- Gambler's Fallacy - idea that prior outcomes can influence an independent probabilistic event
- After a run of reds in a roulette, black will make the overall run more representative (chance as a selfcorrecting process??)

"The urge to find order in the environment appears to be a rather deep-seated human drive." Herb Simon


## The Availability Heuristic

- The frequency of a class or event is often assessed by the ease with which instances of it can be brought to mind
- The problem is that this mental availability might be affected by factors other than the frequency of the class


## Representative Bias (4): Insensitivity to Predictability

- People predict future performance mainly by similarity of description to future results
- For example, predicting future performance as a teacher based on a single practice lesson
- Evaluation percentiles (of the quality of the lesson) were identical to predicted percentiles of 5-year future standings as teachers


## Conjunction Fallacy

- Use of representativeness heuristic: we think that people who exhibit certain characteristics will exhibit other, related characteristics - we think that "like goes with like"
- Example: People were told that Linda majored in philosophy and was a social activist. Then they ranked the probability of 8 statements about Linda.
- Linda is a bank teller
- Linda is a bank teller and a feminist


## Conjunction Fallacy

- $80 \%$ of people rated the statement "Linda is a bank teller and a feminist" as more likely than "Linda is a bank teller"
- This contradicts the fact that the probability of $x$ is greater than the probability of $x$ and $y$ co-occurring (when $x$ and $y$ are independent events)
- When this is pointed out to people, they admit they have made an error

Availability Biases (2):
Effectiveness of a Search Set

- We often form mental "search sets" to estimate how frequent are members of some class
- But, effectiveness of search set might not relate directly to the class frequency
- Which is more prevalent: Words that start with
$r$ or words where $r$ is the $3^{\text {rd }}$ letter?
- Are abstract words such as love more frequent than concrete words such as door?


## Availability Biases (3): Ease of Imaginability

- Instances often need to be constructed on the fly using some rule; the difficulty of imagining instances is used as an estimate of their frequency
- Imaginability might cause overestimation of likelihood of vivid scenarios, and underestimation of the likelihood of difficult-to-imagine ones


## Availability Biases (4): Illusory Correlation

- People tended to overestimate cooccurrence of diagnoses such as paranoia or suspiciousness with features in persons drawn by hypothetical mental patients, such as peculiar eyes
- Subjects might overestimate the correlation due to easier association of suspicion with the eyes than other body parts


## A Trip to the Airport



## The Anchoring and Adjustment Heuristic

- People often estimate by adjusting an initial value until a final value is reached
- Initial values might be due to the problem presentation or due to partial computations
- Adjustments are typically insufficient and are biased towards initial values, the anchor


## Anchoring and Adjustment Biases (1): Insufficient Adjustment

- Anchoring occurs even when initial estimates (e.g., percentage of African nations in the UN) were explicitly made at random by spinning a wheel!
- Anchoring may occur due to incomplete calculation, such as estimating by two high-school student groups
- the expression $8 \times 7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1$ (median answer: 512)
- with the expression $1 \times 2 \times 3 \times 4 \times 5 \times 6 \times 7 \times 8$ (median answer: 2250)
- Anchoring occurs even with outrageously extreme anchors (Quattrone et al., 1984)
- Anchoring occurs even when experts (real-estate agents) estimate real-estate prices (Northcraft and Neale, 1987)


## A Special Type of Bias: Framing

- Risky prospects can be framed in different waysas gains or as losses
- Changing the description of a prospect should not change decisions, but it does, in a way predicted by Tversky and Kahneman's (1979) Prospect Theory
- In Prospect Theory, the negative effect of a loss is larger than the positive effect of a gain
- Framing a prospect as a loss rather than a gain, by changing the reference point, changes the decision by changing the evaluation of the same prospect


## Anchoring/Adjustment Biases (2):

Evaluation of Conjunctive and Disjunctive Events

- People tend to overestimate the probability of conjunctive events (e.g., success of a plan that requires success of multiple steps)
- People underestimate the probability of disjunctive events (e.g. the Birthday Paradox)
- In both cases there is insufficient adjustment from the probability of an individual event



## Decision Making and Explanations

- Pennington \& Hastie
- Complex decision making involves construction of explanations
- Legal Judgment Task
- Varied order of evidence
- People favored the more easily constructed story
- Confidence related to existence of competing explanations


## Satisficing

- Abandon goal of making optimal choice in favor of one that is satisfactory
- Search alternatives until you find a satisfactory one



## Dealing with Complexity

- Elimination of Aspects
- Pick aspect and threshold
- Eliminate sub-threshold members
- Pick next aspect and threshold
- Eliminate sub-threshold members
- (Rinse \& Repeat)



## Decision Making

- Expected Value Theory does not capture subjective value of many goods
- Expected Utility Theory does not capture subjective understanding of probability
- People often use heuristics to make decisions
- Anchoring \& Adjustment
- Availability
- Representativeness
- Use of heuristics can lead to biases \& fallacies
- A\&A $\rightarrow$ Insufficient Adjustment
- Availability $\rightarrow$ Hindsight Bias
- Representativeness $\rightarrow$ Conjunction Fallacy, Gambler's Fallacy


## Adaptive Decision Making

- Payne and colleagues
- Simulations
- Expected Utility
- Tanks under pressure...
- Satisficing
- Elimination of Aspects
- Performed well under time pressure!
- Experiments
- Little time pressure: attempt to use optimal strategies
- Lots of time pressure: use heuristics

