# THE ART (AND SCIENCE?) OF INTERPRETING TABLES 

## BACKGROUND READINGS

- Pollock, Essentials, chs. 3-4


## OUTLINE

1. Components of statistical association
2. Cross-tabulation: format; comparing percentages and means
3. The gamma coefficient
4. Multivariate Relationships
5. Spurious, Enhancement, and Specification Relationships

## The Analytical Challenge: <br> Interpreting and Measuring Relationships

Components of Statistical Association:

1. Form (e.g. positive or negative, varies from -1.0 to +1.0 )
2. Strength (how much $X$ says about $Y$, varies from zero to 1.0)
3. Significance (i.e., probability of null hypothesis, such as $\mathbf{p}<.05$ )

## Arts of Cross-Tabulation

1. Independent variable $(X)$ is the "column" variable
2. Dependent variable ( $\mathbf{Y}$ ) is the "row" variable
3. In case of ordered nominal variables, be sure to array "low-low" values in upper-left hand corner, and "high-high" values in lower right-hand corner
4. Compute percentages along the independent variableNOT of the dependent variable
5. For interpretation, compare percentages across columns at the same value of the dependent variable

## On Setting Up Tables



## Cross-Tabulation I: Comparing Percentages

Table 3-5 Gun Control Opinions, by Partisanship (cross-tabulation)

|  | Party Identification |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| Opinion on Gun Ban | Democrat | Independent | Republican | Total |
| Favor | $52.9 \%$ | $46.6 \%$ | $37.9 \%$ | $46.6 \%$ |
|  | $(314)$ | $(223)$ | $(162)$ | $(699)$ |
| Oppose | $47.1 \%$ | $53.4 \%$ | $62.1 \%$ | $53.4 \%$ |
|  | $(280)$ | $(256)$ | $(265)$ | $(801)$ |
| Total | $100.0 \%$ | $100.0 \%$ | $100.0 \%$ | $100.0 \%$ |
|  | $(594)$ | $(479)$ | $(427)$ | $(1,500)$ |

Note: Question: "Do you favor or oppose a ban on the sale of all handguns, except those that are issued to law enforcement officers?"

## Cross-Tabulation II: Comparing Percentages

| Table 3-6 | Smoking, by Income (cross-tabulation) |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Income Categories |  |  |  |  |  |
|  | $\$ 13,999$ | $\$ 14,000-$ | $\$ 25,000-$ | $\$ 40,000-$ | $\$ 60,000$ |  |
| Smoker? | or less | $\$ 24,999$ | $\$ 39,999$ | $\$ 59,999$ | or more | Total |
| Yes | $32.5 \%$ | $27.0 \%$ | $24.6 \%$ | $21.8 \%$ | $16.4 \%$ | $24.2 \%$ |
|  | $(90)$ | $(62)$ | $(76)$ | $(58)$ | $(52)$ | $(338)$ |
| No | $67.5 \%$ | $73.0 \%$ | $75.4 \%$ | $78.2 \%$ | $83.6 \%$ | $75.8 \%$ |
|  | $(187)$ | $(168)$ | $(233)$ | $(208)$ | $(265)$ | $(1,061)$ |
|  |  |  |  |  |  |  |
| Total | $100.0 \%$ | $100.0 \%$ | $100.0 \%$ | $100.0 \%$ | $100.0 \%$ | $100.0 \%$ |
|  | $(277)$ | $(230)$ | $(309)$ | $(266)$ | $(317)$ | $(1,399)$ |

[^0]Note: Question: "Are you a smoker?"

## Comparing Means: Format I

Table 3-7 Turnout Rates, by State Education Levels (mean comparison, format 1)

|  | State Education Level ${ }^{\mathrm{a}}$ |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | Low | Medium- | Medium- |  |  |
|  | low | high | High | Total |  |
| Mean turnout ${ }^{\mathrm{b}}$ | 45.9 | 53.5 | 56.0 | 62.1 | 54.3 |
| Number of states | $(12)$ | $(15)$ | $(11)$ | (12) | (50) |

Source: State Politics and Policy Data Archive, Illinois Legislative Studies Center, University of Illinois at
Springfield.
ingield.
${ }^{\text {a }}$ Based on the percentage of state residents having at least a high school diploma
Entries are mean turnouts in the 1992 congressional elections.

## Comparing Means: Format II

Table 3-8 Turnout Rates, by State Education Levels (mean comparison, format 2)

| Education Level $^{\mathrm{a}}$ | Mean Turnout ${ }^{\mathrm{b}}$ |
| :--- | :---: |
| Low | 45.9 |
|  | $(12)$ |
| Medium-low | 53.5 |
|  | $(15)$ |
| Medium-high | 56.0 |
|  | $(11)$ |
| High | 62.1 |
|  | $(12)$ |
|  |  |
| Total | 54.3 |
|  | $(50)$ |

Source: State Politics and Policy Data Archive.
${ }^{\text {a }}$ Based on percentage of state residents having at least a high
school diploma.
${ }^{\text {b }}$ Entries are mean turnouts in the 1992 congressional elections.

# Cross-Tabulation III: Comparing Percentages 

Table 3-9 Gay Rights Opinions, by Age (cross-tabulation)

| Opinion on <br> Gay Rights Law | $18-30$ | $31-40$ | $41-50$ | $51-65$ | over 65 | Totals |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Favor | $69.2 \%$ | $60.9 \%$ | $68.5 \%$ | $63.4 \%$ | $59.0 \%$ | $63.9 \%$ |
|  | $(157)$ | $(220)$ | $(200)$ | $(177)$ | $(164)$ | $(918)$ |
| Oppose | $30.8 \%$ | $39.1 \%$ | $31.5 \%$ | $36.6 \%$ | $41.0 \%$ | $36.1 \%$ |
|  | $(70)$ | $(141)$ | $(92)$ | $(102)$ | $(114)$ | $(519)$ |
|  |  |  |  |  |  |  |
| Totals |  |  |  |  |  |  |
|  | $100.0 \%$ | $100.0 \%$ | $100.0 \%$ | $100.0 \%$ | $100.0 \%$ | $100.0 \%$ |
|  | $(227)$ | $(361)$ | $(292)$ | $(279)$ | $(278)$ | $(1,437)$ |

Source: 1996 National Election Study.
Note: Question: "Do you favor or oppose laws to protect homosexuals against job discrimination?"

## The Gamma Coefficient

1. Appropriate for ordered nominal variables
2. Provides measure of form (positive or negative) and of strength (coefficient varies from $\mathbf{- 1 . 0}$ to $+\mathbf{1 . 0}$ )
3. Sample computations for $2 \times 2$ table
4. Does not provide measure of "significance"

## Example and Sample Computation: Gun Control Attitudes and Gender

|  | Gender |  |  |
| :--- | :--- | :--- | :--- |
| Gun Ban?__ | Male | Female | Total |
| Oppose | $449[\mathrm{a}]$ | $358[\mathrm{~b}]$ | 807 |
| Favor | $226[\mathrm{c}]$ | $481[\mathrm{~d}]$ | 707 |
| Total | 675 | 839 | 1,514 |

## Computing Gamma

(AKA Yule's $\mathbf{Q}$ for $\mathbf{2 x} \mathbf{2}$ tables):

$$
\begin{aligned}
\Gamma & =\text { Yule's } \mathrm{Q}=(\mathrm{ad}-\mathrm{bc}) /(\mathrm{ad}+\mathrm{bc}) \\
& =(449 \times 481-226 \times 358) /(449 \times 481+226 \times 358) \\
& =+.455
\end{aligned}
$$

Thus a measure of form and strength

VISURLIZINE GAMMA

$\because$ SAME-DERERCD PAIRS
(y)

$$
10
$$ me

$\mu$ :

$\therefore$ REVERSE-ORDEREA DAIRS

DEFINING GAMMA

$$
\begin{aligned}
\partial & =\frac{\text { SAME - REversE }}{\text { SAME }- \text { REvERSE }} \\
& =\frac{n_{s}-n_{r}}{n_{s}+n_{r}}
\end{aligned}
$$

EXCLUDING TIES
THUS A MEASURE OF STRENGTH ANT FORM

## MULTIVARIATE RELATIONSHIPS

- The "How Else" Question
- Spurious, Enhancement, and Specification Relationships (a.k.a. "Interaction")
- Example 1: Race, Education, and Turnout
- Example 2: Gender, Race, and Support for the Death Penalty


## Examining Relationship between $\mathbf{Y}$ and $\mathbf{X}$,

 Controlling for a Rival Cause Z
## Potential Outcomes:

Spurious relationship- $\mathbf{Y}$ a function of $\mathbf{Z}$ and not X
Enhancement relationship-Y a function of both $X$ and $Z$
Specification relationship-i.e., control variable $(Z)$ specifies or defines conditions under which $X$ affects $Y$ [also known as "interaction"]

Figure 4-1 Spurious Relationship Between X and Y (arrow diagram)


Figure 4-3 Enhancement Relationships Between $X, Y$ and $Z$ (arrow diagram)


Figure 4-5 Specification Relationships Between $\mathrm{X}, \mathrm{Y}$ and Z (arrow diagram)


82 The Essentials of Political Analysis

| Table 4-1 | Relationship Between Race $(\mathrm{X})$ and Turnout (Y) |  |  |
| :--- | :---: | :---: | :---: |
| Race (X) |  |  |  |
|  | White | Black | Total |
|  | $22.0 \%$ | $32.2 \%$ | $23.2 \%$ |
|  | $(290)$ | $(55)$ | $(345)$ |
| Yes | 78.0 | 67.8 | 76.8 |
|  | $(1,027)$ | $(116)$ | $(1,143)$ |
|  |  |  |  |
| Total |  | $100.0 \%$ | $100.0 \%$ |
|  | $(1,317)$ | $(171)$ | $100.0 \%$ |
|  | Source: National Election Study, 1996: Pre-and Post-election Survey; Steven J. |  |  |

Source: National Election Study, 1996: Pre- and Post-election Survey, Steven Rosenstone, Donald R. Kinder, Warren E. Miller, and the National Election Studies (Ann Arbor: University of Michigan, Center for Political Studies, and Inter-university Consortium for Political and Social Research, 1997).

Table 4-2 Relationship Between Race $(X)$ and Turnout $(Y)$, Controlling for Education $(Z)$

| Voted? (Y) | Level of Education (Z) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | High school or less |  |  | More than high school |  |  |
|  | Race (X) |  | Total | Race (X) |  | Total |
|  | White | Black |  | White | Black |  |
| No | 32.8\% | 40.4\% | 33.9\% | 14.1\% | 20.8\% | 14.7\% |
|  | (184) | (40) | (224) | (106) | (15) | (121) |
| Yes | $67.2 \%$ | $59.6 \%$ | $66.1 \%$ | 85.9\% | $79.2 \%$ | $85.3 \%$ |
|  | (377) | (59) | (436) | (647) | (57) | (704) |
| Total | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% |
|  | (561) | (99) | (660) | (753) | (72) | (825) |

Source: 1996 National Election Study.

Table 4-2 Relationship Between Race $(X)$ and Turnout $(Y)$, Controlling for Education $(Z)$

| Voted? (Y) | Level of Education (Z) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | High school or less |  |  | More than high school |  |  |
|  | Race (X) |  | Total | Race (X) |  | Total |
|  | White | Black |  | White | Black |  |
| No | 32.8\% | 40.4\% | 33.9\% | 14.1\% | 20.8\% | 14.7\% |
|  | (184) | (40) | (224) | (106) | (15) | (121) |
| Yes | $67.2 \%$ | $59.6 \%$ | $66.1 \%$ | 85.9\% | $79.2 \%$ | $85.3 \%$ |
|  | (377) | (59) | (436) | (647) | (57) | (704) |
| Total | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% |
|  | (561) | (99) | (660) | (753) | (72) | (825) |

Source: 1996 National Election Study.

Table 4-3 Relationship Between Gender $(X)$ and Support for the Death Penalty $(Y)$, Controlling for Race (Z)



[^0]:    Source: 1996 National Election Study.

